

M217 Geometry

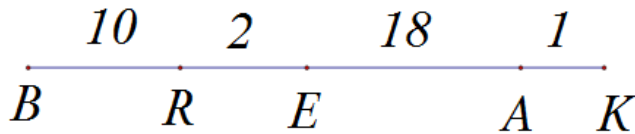
# Section 9-6: Geometric Probability

Geometric probability is .... **The probability of an event based on a ratio of geometric measures (such as length or area)**

We have three different models

1) Using Length

Let's say that I randomly choose a point on the line below.



a. What is the probability the point is on  $\overline{BR}$ ?

The probability is  $\frac{10}{31} \approx .3226$

b. What is the probability the point is NOT on  $\overline{BR}$ ?

The probability is  $\frac{2+18+1}{31} = \frac{21}{31} \approx 0.6774$  or  $1-0.3226= 0.6774$

c. What is the probability the point is on  $\overline{RA}$ ?

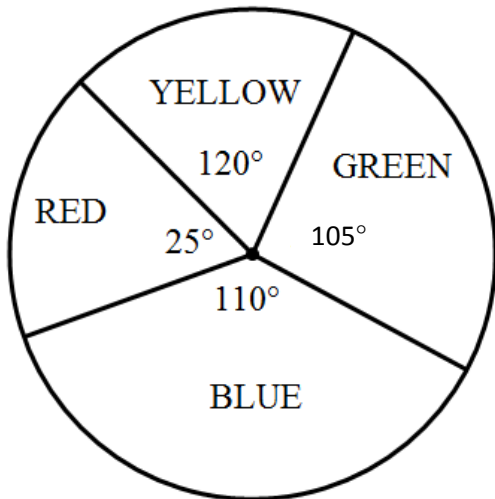
The probability is  $\frac{2+18}{31} = \frac{20}{31} \approx 0.6452$

d. What is the probability the point is NOT on  $\overline{RA}$ ?

The probability is  $\frac{10+1}{31} = \frac{11}{31} \approx 0.3548$  or  $1-0.6452=0.3548$

2) Using Angle Measure

Let's say I have a spinner like the one below...



1. Which color is more likely the spinner to land on?

**YELLOW**

2. Which color is the spinner least likely to land on?

**RED**

3. Find the probability the spinner lands on BLUE?

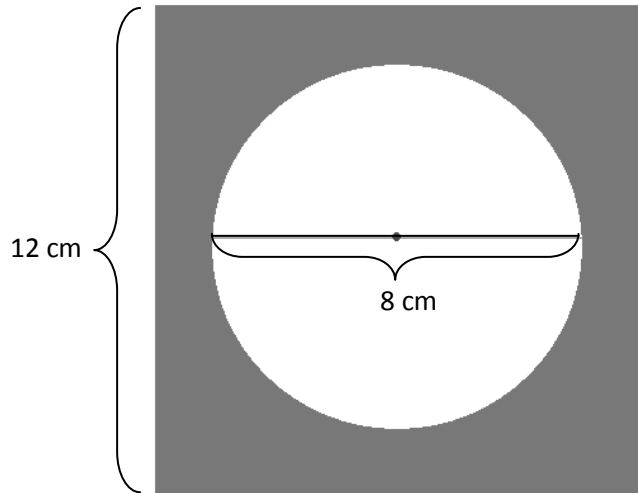
$$\frac{110^\circ}{360^\circ} = \frac{11}{36} \approx 0.3055$$

4. Find the probability the spinner lands on YELLOW or RED?

$$\frac{120^\circ + 25^\circ}{360^\circ} = \frac{145}{360} = \frac{29}{72} \approx 0.4028$$

**3) Using Area to find probability**

1) Let's say I throw a dart at the image below. Let's say I hit somewhere inside the square....



a) What is the area of the circle?  
 $A = \pi r^2 = \pi(4)^2 = 16\pi \text{ cm}^2 \approx 50.27 \text{ cm}^2$

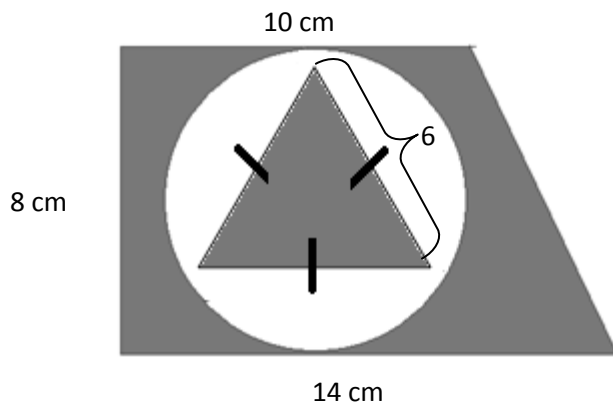
b) What is the area of the square?  
 $A = bh = 12 * 12 = 144 \text{ cm}^2$

c) What is the area of the shaded region?  
 $A = \text{Square} - \text{Circle}$   
 $= 144 \text{ cm}^2 - 16\pi \text{ cm}^2$   
 $\approx 93.73 \text{ cm}^2$

d) What is the probability of the dart landing in the circle?  
 $\frac{50.27}{144} \approx 0.3491$

e) What is the probability of landing in the shaded region?  
 $\frac{93.73}{144} \approx 0.6509$

2) Let's say I throw a dart at the image below. Let's say I hit somewhere inside the trapezoid...



a) What is the area of the trapezoid  
 $A = \frac{1}{2}(b_1 + b_2)h = \frac{1}{2}(10 + 14) * 8 = \frac{1}{2}(24)(8)$   
 $= \frac{192}{2} = 96 \text{ cm}^2$

b) What is the area of the circle?  
 $A = \pi r^2 = \pi(4)^2 = 16\pi \text{ cm}^2 \approx 50.27 \text{ cm}^2$

c) What is the area of the Equilateral Triangle?  
 $A = \frac{s^2\sqrt{3}}{4} = \frac{(6)^2\sqrt{3}}{4} = \frac{36\sqrt{3}}{4} \text{ cm}^2 \approx 15.59 \text{ cm}^2$

d) What is the probability of the dart landing in the shaded region?

e) What is the probability of the dart landing in the equilateral triangle?

$A = \text{Trap} - \text{Circle} + \Delta = 96 - 50.27 + 15.59 = 61.323 \text{ cm}^2$   
 $\text{probability} = \frac{61.323}{96} \approx 0.6388$

$\text{probability} = \frac{15.59}{96} \approx 0.1624$

### PRACTICE PROBLEMS

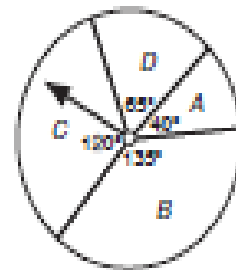
A point is randomly chosen on  $\overline{AD}$ . Find the fractional probability of each event.



- The point is on  $\overline{AB}$ .  $\frac{5}{12}$
- The point is on  $\overline{AD}$ .  $1$

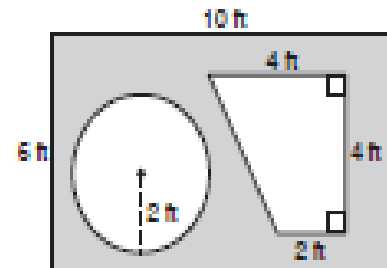
- The point is on  $\overline{BD}$ .  $\frac{7}{12}$
- The point is not on  $\overline{BC}$ .  $\frac{2}{3}$

Use the spinner to find the fractional probability of each event.



- the pointer landing in region C  $\frac{1}{3}$
- the pointer landing in region A  $\frac{1}{9}$
- the pointer not landing in region D  $\frac{59}{72}$
- the pointer landing in regions A or B  $\frac{35}{72}$

Find the probability that a point chosen randomly inside the rectangle is in each given shape. Round answers to the nearest hundredth.



- the circle  $0.21$
- the trapezoid  $0.20$
- the circle or the trapezoid  $0.41$
- not the circle and the trapezoid  $0.59$

